



# COLLEGE of ENGINEERING AND PHYSICAL SCIENCES

SCHOOL OF COMPUTER SCIENCE

## MSc Defence

**Tuesday August 28, 2018 at 10AM in MacKinnon, Room 313**

*Constructing de Bruijn Sequences by Concatenating Cycles of  
Feedback Shift Registers*

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### **Abstract:**

A universal cycle for a set  $S$  of strings is a circular sequence of length  $|S|$  that contains every element of  $S$  as a substring exactly once. In this thesis we introduce sufficient conditions for when an ordering of universal cycles for disjoint sets can be concatenated to obtain a universal cycle for the union of those sets. A  $k$ -ary de Bruijn sequence of order  $n$  is a universal cycle where  $S$  is the set of all  $k$ -ary strings of length  $n$ . De Bruijn sequences can be constructed a variety of different ways, but we will focus on constructing de Bruijn sequences by concatenating universal cycles. We use our conditions to prove the validity of three new de Bruijn sequences, two of which are based on concatenating connectives, and one is based on concatenating necklaces. Then we introduce a class of new  $k$ -ary de Bruijn sequence that are based on concatenating cycles of feedback shift registers. Finally, we show that a brute force algorithm can generate the class of de Bruijn sequences in  $O(k^2n^2)$ -amortized time per universal cycle.